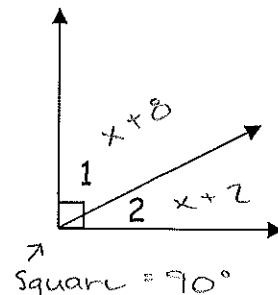


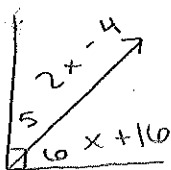
Complementary Angles - add up to 90°



Ex. 1 In the picture above, $m\angle 1 = x + 8$ and $m\angle 2 = x + 2$. Find x and $m\angle 2$.

$$\begin{aligned}
 x + 8 + x + 2 &= 90 & x &= 40 & 40 + 2 &= 42 \\
 2x + 10 &= 90 & 2 &= 42 \\
 \frac{2x + 10}{2} &\quad \frac{-10}{-10} \\
 \hline
 \frac{2x}{2} &= 40
 \end{aligned}$$

Ex. 2 $\angle 5$ is the complement of $\angle 6$. If $m\angle 5 = 2x - 4$ and $m\angle 6 = x + 16$, find x and $m\angle 6$.



$$\begin{aligned}
 2x - 4 + x + 16 &= 90 \\
 3x + 12 &= 90 \\
 \frac{3x + 12}{3} &\quad \frac{-12}{-12} \\
 \hline
 \frac{3x}{3} &= 26 \\
 x &= 26 \\
 6 &= 42
 \end{aligned}$$

$$26 + 16 = 42$$

Notes 2-4

Complementary and Supplementary Angles

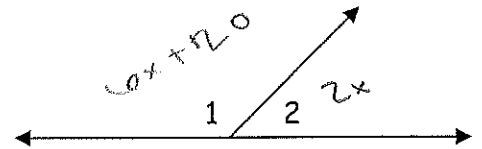
Supplementary Angles -

angles that add up to 180°

Straight line = 180°

Linear Pair -

2 angles that form a straight line



Ex. 3 In the picture above, $m\angle 1 = 6x + 20$ and $m\angle 2 = 2x$. Find x and $m\angle 1$.

$$x = 20$$

$$1 = 140$$

$$6(20) + 20$$

$$120 + 20$$

$$140$$

$$6x + 20 + 2x = 180$$

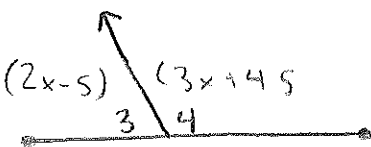
$$8x + 20 = 180$$

$$\quad -20 \quad -20$$

$$\frac{8x}{8} = \frac{160}{8}$$

$$x = 20$$

Ex. 4 $\angle 3$ and $\angle 4$ are a linear pair. $m\angle 3 = 2x - 5$ and $m\angle 4 = 3x + 45$. Find x and $m\angle 4$.



$$2x - 5 + 3x + 45 = 180$$

$$5x + 40 = 180$$

$$5x = 140$$

$$x = 28$$

$$x = 28^\circ$$

$$4 = 129^\circ$$

Ex 5 In the picture to the right, find x and $m\angle ABE$.

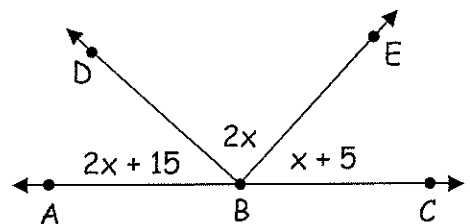
$$2x + 15 + 2x + x + 5 = 180$$

$$5x + 20 = 180$$

$$5x = 160$$

$$x = 32$$

$$ABE = 143^\circ$$



$$2(32) + 15 = 79^\circ$$

$$2(32) = 64^\circ > 143$$

Use the Four-Step Problem-Solving Procedure for each problem. Write your final answers in the appropriate blank.

Complementary Angles

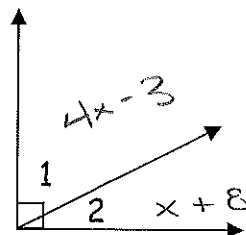
1. $m\angle 1 = 4x - 3$ and $m\angle 2 = x + 8$. Find x and $m\angle 2$.

$$x = 17 \qquad x = 15 \qquad 4x - 3 + x + 8 = 90$$

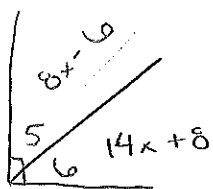
$$m\angle 2 = 25 \qquad (15) + 8 = 23 \qquad 5x + 5 = 90$$

$$\qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad -5 \quad -5$$

$$\qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \frac{5x}{5} = \frac{85}{5} = 17$$



2. $\angle 5$ is the complement of $\angle 6$. If $m\angle 5 = 8x - 6$ and $m\angle 6 = 14x + 8$, find x and $m\angle 6$.



$$8x - 6 + 14x + 8 = 90$$

$$22x + 2 = 90$$

$$\quad \quad -2 \quad -2$$

$$22x = 88 = 4$$

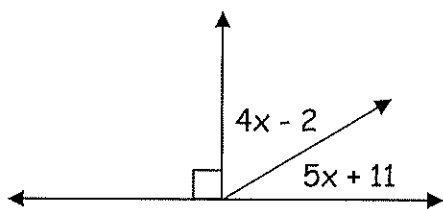
$$\quad \quad \frac{22}{22} \quad \frac{88}{22}$$

$$14(4) + 8 = 56 + 8 = 64$$

$$x = 4$$

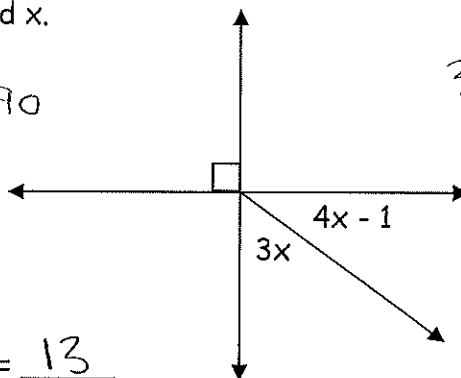
$$m\angle 6 = 64$$

3. Find x .



$$x = 9$$

4. Find x .



$$x = 13$$

$$3x + 4x - 1 = 90$$

$$7x - 1 = 90$$

$$\quad \quad +1 \quad +1$$

$$7x = 91$$

$$x = 13$$

Supplementary Angles/Linear Pair

5. $m\angle 1 = 2x + 4$ and $m\angle 2 = 6x + 20$. Find x and $m\angle 1$.

$$x = 19.5$$

$$m\angle 1 = 43$$

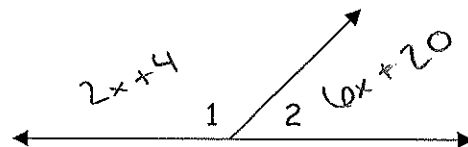
$$2x + 4 + 6x + 20 = 180$$

$$8x + 24 = 180$$

$$\quad \quad -24 \quad -24$$

$$8x = 156$$

$$\quad \quad \quad \quad \quad 2(19.5) + 4$$

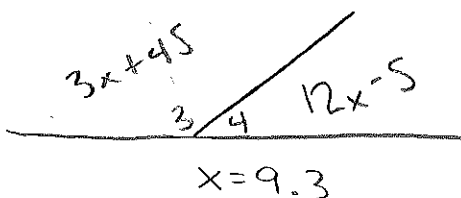


6. $\angle 3$ and $\angle 4$ are a linear pair. $m\angle 3 = 12x - 15$ and $m\angle 4 = 3x + 45$. Find x and $m\angle 4$.

$$x = 9.3$$

$$m\angle 4 = 106.6$$

$$12(9.3) - 5$$



$$3x + 45 + 12x - 5 = 180$$

$$15x + 40 = 180$$

$$\quad \quad -40 \quad -40$$

$$15x = 140$$

7. In the picture to the right, find x and $m\angle ABE$.

$$x = \underline{25}$$

$$m\angle ABE = \underline{145}$$

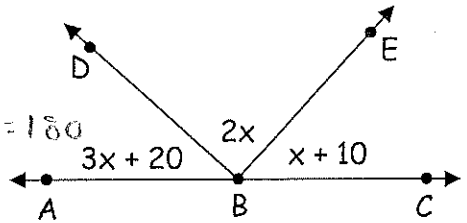
$$\begin{array}{r} 180 \\ - 35 \\ \hline 145 \end{array}$$

$$25 + 10 = 35$$

$$3x + 20 + 2x + x + 10 = 180$$

$$\begin{array}{r} 6x + 30 = 180 \\ - 30 \quad - 30 \\ \hline \end{array}$$

$$\begin{array}{r} 6x = 150 \\ \div 6 \\ \hline x = 25 \end{array}$$



8. In the picture to the right, find x and $m\angle ABC$.

$$x = \underline{12.5}$$

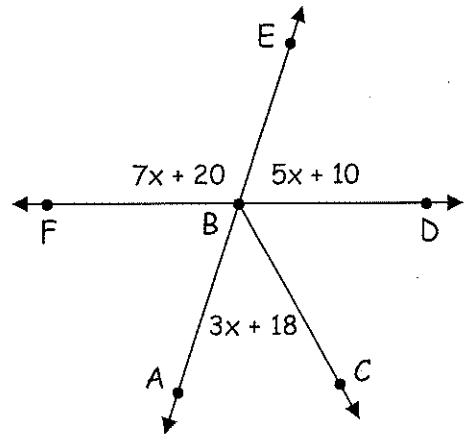
$$m\angle ABC = \underline{55.5}$$

$$3(54) + 18$$

$$\begin{array}{r} 12x + 30 = 180 \\ - 30 \quad - 30 \\ \hline 12x + 150 \end{array}$$

$$\begin{array}{r} 3x + 18 = 180 \\ - 18 \quad - 18 \\ \hline \end{array}$$

$$\begin{array}{r} 7x + 20 + 5x + 10 = 180 \\ 12x + 30 = 180 \end{array}$$



9. $\overrightarrow{TM} \perp \overrightarrow{RS}$, $m\angle QMS = 58^\circ$. Find the measure of each angle.

a) $m\angle TMQ = \underline{32^\circ}$

b) $m\angle RMP = \underline{58^\circ}$

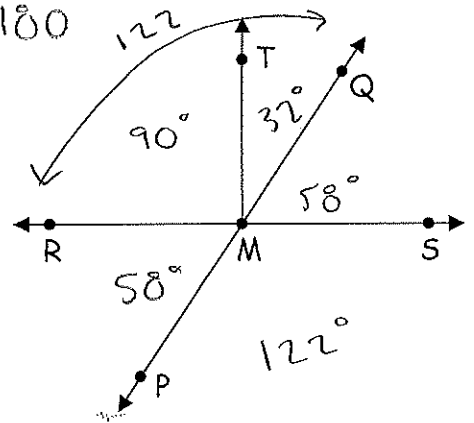
c) $m\angle SMP = \underline{122^\circ}$

d) $m\angle PMT = \underline{148^\circ}$

$$\begin{array}{r} 180 \\ - 58 \\ \hline 122 \end{array}$$

$$\begin{array}{r} 90 \\ - 58 \\ \hline \end{array}$$

$$\begin{array}{r} 58 \\ + 90 \\ \hline 148 \end{array}$$



10. $m\angle AEC = 3x + 5$ and $m\angle DEF = 2x - 15$. Find $m\angle DEF$, $m\angle DEB$, and $m\angle CEB$.

$$m\angle DEF = \underline{25^\circ}$$

$$m\angle DEB = \underline{65^\circ}$$

$$m\angle CEB = \underline{115^\circ}$$

$$3x + 5 + x + 2x - 15 = 180$$

$$\begin{array}{r} 6x - 10 = 180 \\ + 10 \quad + 10 \\ \hline \end{array}$$

$$6x = 190$$

