

Rotation:

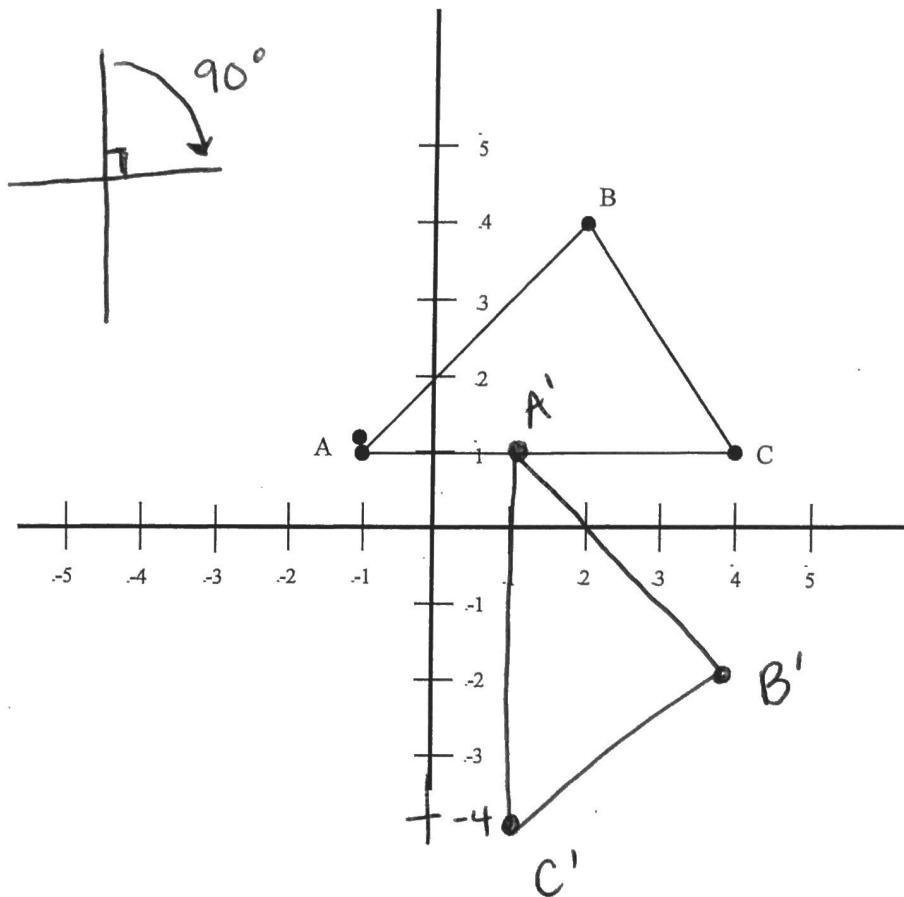
Ex 1: Given $\triangle ABC$ with points $A(-1, 1)$, $B(2, 4)$, $C(4, 1)$, rotate $\triangle ABC$ 90° clockwise about the origin.

(A) Graph

$A(-1, 1)$

$B(2, 4)$

$C(4, 1)$



(B) Vertex matrices

		<u>Given image</u>					<u>Transformed image</u>		
		A	B	C			A'	B'	C'
x	$\left[\begin{array}{ccc} -1 & 2 & 4 \\ 1 & 4 & 1 \end{array} \right]$				\longrightarrow	x	$\left[\begin{array}{ccc} 1 & 4 & 1 \\ 1 & -2 & -4 \end{array} \right]$		
y						y			

(C) Algebraic (arrow) rule

$$(x, y) \rightarrow (y, -x)$$

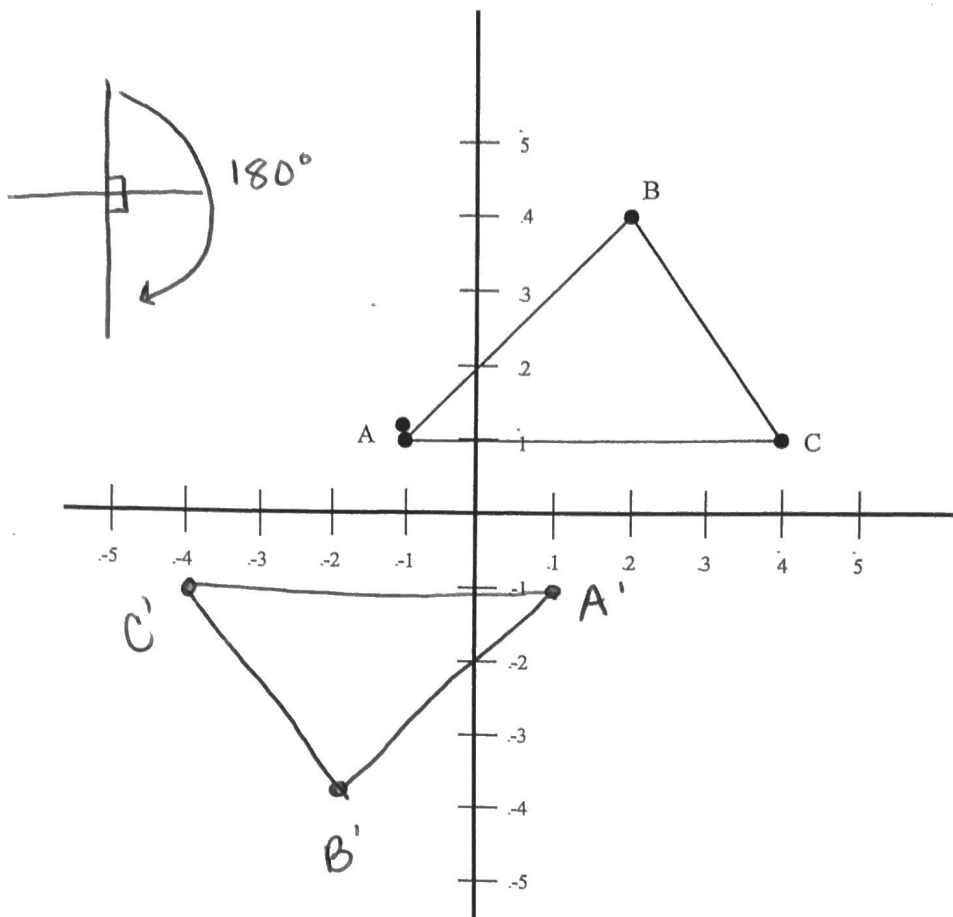
Ex 2: Given $\triangle ABC$ with points $A(-1, 1)$, $B(2, 4)$, $C(4, 1)$, rotate $\triangle ABC$ 180° clockwise about the origin.

(A) Graph

$$A(-1, 1)$$

$$B(2, 4)$$

$$C(4, 1)$$



(B) Vertex matrices

Given image

$$\begin{array}{c} x \\ y \end{array} \begin{array}{ccc} A & B & C \\ \left[\begin{array}{ccc} -1 & 2 & 4 \\ 1 & 4 & 1 \end{array} \right] \end{array}$$

Transformed image

$$\begin{array}{c} x \\ y \end{array} \begin{array}{ccc} A' & B' & C' \\ \left[\begin{array}{ccc} 1 & -2 & -4 \\ -1 & -4 & -1 \end{array} \right] \end{array}$$

(C) Algebraic (arrow) rule

$$(x, y) \longrightarrow (-x, -y)$$

Notes 2.4

Rotations

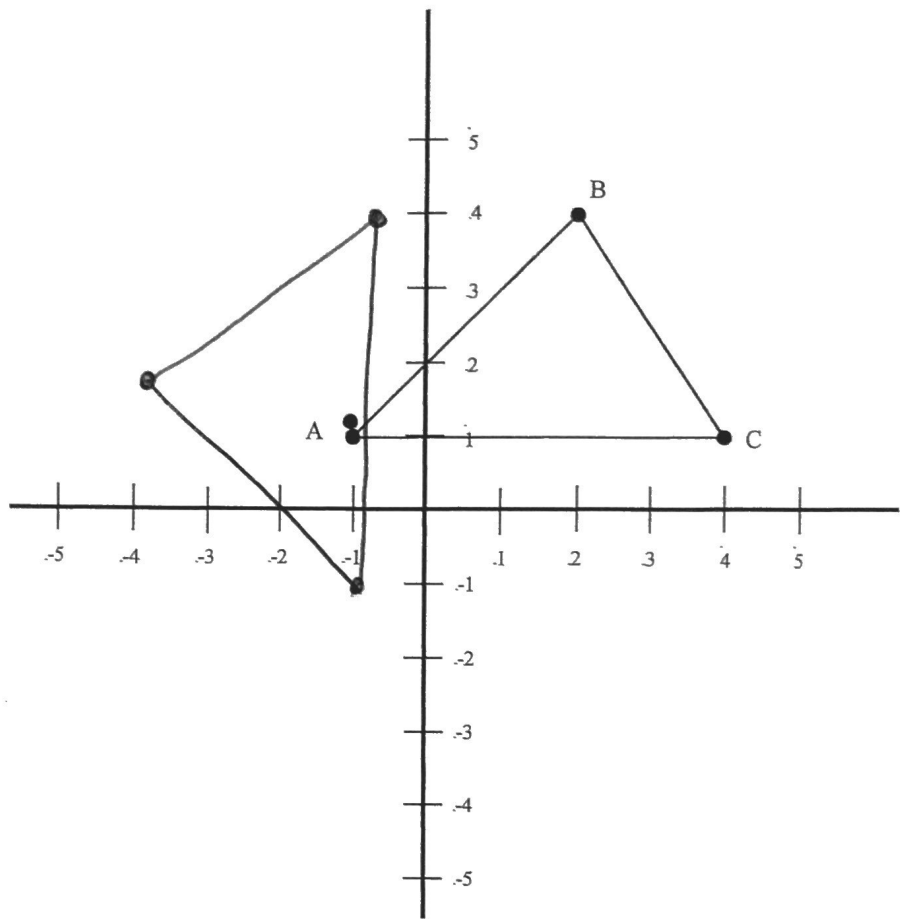
Ex 3: Given $\triangle ABC$ with points $A(-1, 1)$, $B(2, 4)$, $C(4, 1)$, rotate $\triangle ABC$ 270° clockwise about the origin.

(A) Matrices

$$A(-1, 1)$$

$$B(2, 4)$$

$$C(4, 1)$$



(B) Vertex matrices

Given image

$$\begin{matrix} X & A & B & C \\ Y & \begin{bmatrix} -1 & 2 & 4 \\ 1 & 4 & 1 \end{bmatrix} \end{matrix}$$

Transformed image

$$\begin{matrix} X & A' & B' & C' \\ Y & \begin{bmatrix} -1 & -4 & -1 \\ -1 & 2 & 4 \end{bmatrix} \end{matrix}$$

(C) Algebraic (arrow) rule

$$(x, y) \rightarrow (-y, x)$$

Review Table

Clockwise Rotation	Counter Clockwise Rotation	Algebraic Rule
90°	270°	$(x, y) \rightarrow (y, -x)$
180°	180°	$(x, y) \rightarrow (-x, -y)$
270°	90°	$(x, y) \rightarrow (-y, x)$

Ex 4: $\triangle XYZ$ with $X(2, -1)$, $Y(4, -3)$, $Z(-2, 1)$. Rotate 90° counterclockwise. Write each vertex matrix.

Ex 5: Quadrilateral $ABCD$ with $A(3, 1)$, $B(6, -2)$, $C(5, -5)$ and $D(1, -6)$. Reflect across the x -axis and then rotate the figure 180° . Write each vertex matrix.

Ex 6: Pentagon $MNOPQ$ with $M(-1, 0)$, $N(-1, 5)$, $O(0, 7)$, $P(1, 5)$, and $Q(1, 0)$. Dilate by $r = 3$ and then rotate the figure 90° clockwise. Write each vertex matrix.